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> with(LinearAlgebra):
> K := Matrix([[ -k1-k2,0,0,0],[+k1,0,0,0],[+k2,0,-k3,+k4],[0,0,+k3,-k4]]);
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$$K := \begin{bmatrix} -k1 - k2 & 0 & 0 & 0 \\ k1 & 0 & 0 & 0 \\ k2 & 0 & -k3 & k4 \\ 0 & 0 & k3 & -k4 \end{bmatrix}$$

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> E := Eigenvectors(K);
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$$E := \begin{bmatrix} -k3 - k4 \\ 0 \\ 0 \\ -k1 - k2 \end{bmatrix}, \begin{bmatrix} 0 & 0 & 0 & \frac{(k1 + k2)(-k3 - k4 + k1 + k2)}{k3 k2} \\ 0 & 0 & 1 & -\frac{k1(-k3 - k4 + k1 + k2)}{k3 k2} \\ -1 & 1 & 0 & -\frac{k1 + k2 - k4}{k3} \\ 1 & \frac{k3}{k4} & 0 & 1 \end{bmatrix}$$

```
> v := E[1];
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$$v := \begin{bmatrix} -k3 - k4 \\ 0 \\ 0 \\ -k1 - k2 \end{bmatrix}$$

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> X := E[2];
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$$X := \begin{bmatrix} 0 & 0 & 0 & \frac{(k1 + k2)(-k3 - k4 + k1 + k2)}{k3 k2} \\ 0 & 0 & 1 & -\frac{k1(-k3 - k4 + k1 + k2)}{k3 k2} \\ -1 & 1 & 0 & -\frac{k1 + k2 - k4}{k3} \\ 1 & \frac{k3}{k4} & 0 & 1 \end{bmatrix}$$

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> L :=
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DiagonalMatrix([exp(v[1]*t),exp(v[2]*t),exp(v[3]*t),exp(v[4]*t)]);
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$$L := \begin{bmatrix} e^{((-k3 - k4)t} & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & e^{((-k1 - k2)t} \end{bmatrix}$$

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> c0 := Vector ([Ao,0,0,0]);
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$$c0 := \begin{bmatrix} A0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

> **ct := X . L . MatrixInverse(X) . c0;**
ct :=

$$\begin{aligned} & [e^{((-k1-k2)t)} A0] \\ & \left[\left(\frac{k1}{k1+k2} - \frac{k1 e^{((-k1-k2)t)}}{k1+k2} \right) A0 \right] \\ & \left[\left(\frac{e^{((-k3-k4)t)} k3 k2}{(-k3-k4+k1+k2)(k3+k4)} + \frac{k2 k4}{(k1+k2)(k3+k4)} \right. \right. \\ & \quad \left. \left. - \frac{(k1+k2-k4) e^{((-k1-k2)t)} k2}{(k1+k2)(-k3-k4+k1+k2)} \right) A0 \right] \\ & \left[\left(-\frac{e^{((-k3-k4)t)} k3 k2}{(-k3-k4+k1+k2)(k3+k4)} + \frac{k3 k2}{(k1+k2)(k3+k4)} \right. \right. \\ & \quad \left. \left. + \frac{e^{((-k1-k2)t)} k3 k2}{(k1+k2)(-k3-k4+k1+k2)} \right) A0 \right] \end{aligned}$$

> **ctA := ct[1];**

$$ctA := e^{((-k1-k2)t)} A0$$

> **ctB := ct[2];**

$$ctB := \left(\frac{k1}{k1+k2} - \frac{k1 e^{((-k1-k2)t)}}{k1+k2} \right) A0$$

> **ctC := ct[3];**

$$\begin{aligned} ctC := & \left(\frac{e^{((-k3-k4)t)} k3 k2}{(-k3-k4+k1+k2)(k3+k4)} + \frac{k2 k4}{(k1+k2)(k3+k4)} \right. \\ & \left. - \frac{(k1+k2-k4) e^{((-k1-k2)t)} k2}{(k1+k2)(-k3-k4+k1+k2)} \right) A0 \end{aligned}$$

> **ctD := ct[4];**

$$\begin{aligned} ctD := & \left(-\frac{e^{((-k3-k4)t)} k3 k2}{(-k3-k4+k1+k2)(k3+k4)} + \frac{k3 k2}{(k1+k2)(k3+k4)} \right. \\ & \left. + \frac{e^{((-k1-k2)t)} k3 k2}{(k1+k2)(-k3-k4+k1+k2)} \right) A0 \end{aligned}$$

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