
Covalent Inhibition Kinetics

Application to EGFR Kinase

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Covalent inhibition of protein kinases: Case study

ENZYME

**Epidermal Growth Factor
Receptor (EGFR) Kinase**

9 **COVALENT** KINASE INHIBITORS

Gilotrif® (afatinib)
Dacomitinib
Neratinib

...
...

GOAL

Determine basic biochemical characteristics of inhibitors:

- (1) initial binding affinity: K_i
- (2) chemical reactivity: K_{inact}

REFERENCE

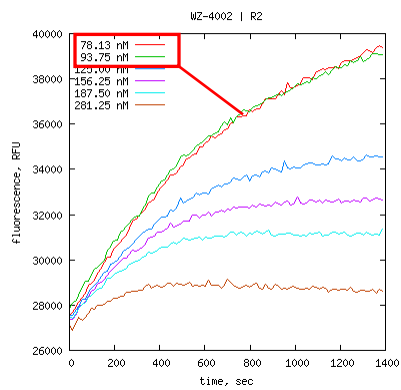
Schwartz, P.; Kuzmic, P. *et al.* (2014)
Proc. Natl. Acad. Sci. USA. **111**, 173-178.



**PRELIMINARIES:
ASSESSMENT OF RAW DATA**

Reproducibility: Fixed vs. optimized concentrations

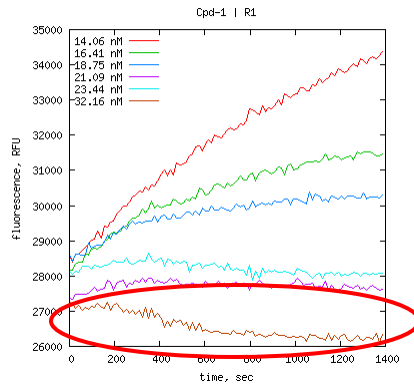
GLOBAL FIT OF COMBINED TRACES REQUIRES THAT CONCENTRATIONS ARE CONSISTENT



- Both of these inhibitor concentrations cannot be correct.
- Or can they ... ?
- We will treat inhibitor concentrations as adjustable parameters.

Outliers – Anomalous reaction progress

ABOUT 2% (10 / 400) OF KINETIC TRACES IN THIS DATA SET ARE CLEARLY **ANOMALOUS**



Exclude this curve before analysis.

Optimal maximum inhibitor concentrations

IDENTICAL MAXIMUM CONCENTRATION **WOULD NOT WORK**

COMPOUND	[I] _{max} nM
Afatinib	35.2
CL-387785	375.0
Cpd-2	62.5
Cpd-3	187.5
Cpd-4	7500.0
Cpd-5	1500.0
Dacomitinib	93.8
Neratinib	46.9
WZ-4002	187.5

- Maximum concentrations are based on preliminary experiments (IC₅₀).

Inhibitor vs. enzyme concentration: "Tight Binding" – Part 1

Compound	K_i^* , nM
CI-1033	1.6 ± 0.7
dacomitinib	18 ± 1
afatinib	4.4 ± 0.4
neratinib	4.0 ± 0.5
1	3.2 ± 0.5
CL-387785	180 ± 11
2	63 ± 5
3	84 ± 3
4	2200 ± 100
5	430 ± 30
WZ-4002	340 ± 20

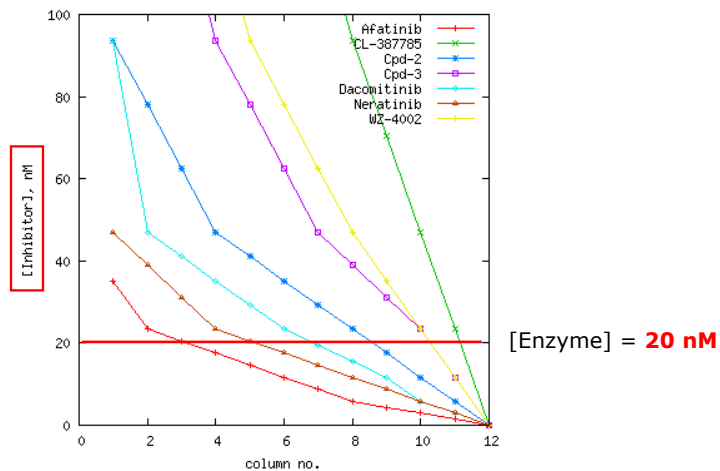
- "Tight binding" is **not** a property of the **inhibitors**.
- "Tight binding" has to do with **assay conditions**.
- "TB" means that $[E]_0 \approx K_i$ or even $[E]_0 > K_i$

$$[E]_0 = 20 \text{ nM}$$

Is $[E]_0$ is **very much lower** than K_i ?

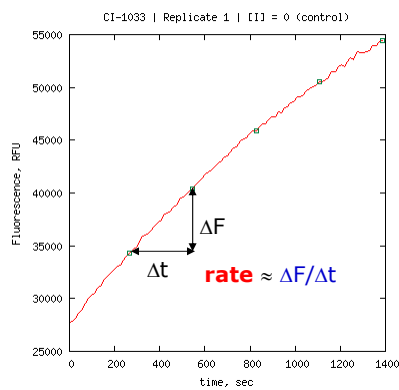
Table S 1: Apparent inhibition constants determined from the fit of *initial reaction rates* to the Morrison Eqn

Inhibitor vs. enzyme concentration: "Tight Binding" – Part 2

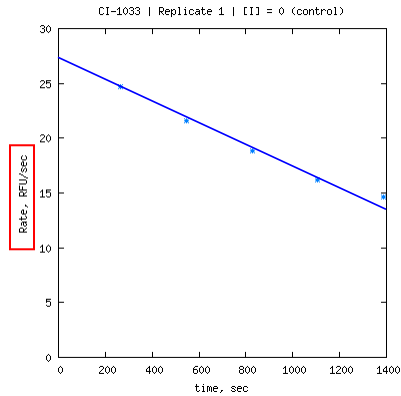


- Inhibitor and enzyme concentrations are comparable.
- **Inhibitor depletion** does occur.

Substrate-only control: Linear or nonlinear?



Guess how much the slope (i.e., rate) changes between marked time points?



Reaction rate changes by **almost 50%** from start to finish: **NONLINEAR**.

Assessment of data: Implications for method of analysis

- Some **curves** will need to be **excluded**, preferably **automatically**.
- **Concentrations** will need to be treated as "unknown" parameters.

- **Inhibition depletion** does occur ("tight binding").
- **Substrate depletion** does occur (**nonlinear control** curve).

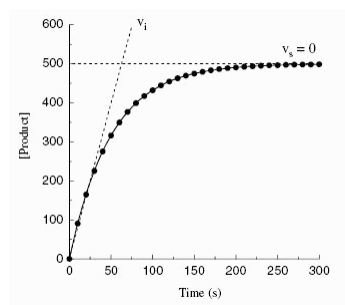
These facts will determine the choice of the mathematical model.

**MATHEMATICAL MODELS:
ALGEBRAIC VS. DIFFERENTIAL EQUATIONS**

“Traditional” method to analyze covalent inhibition data: Step 1

Copeland, R. (2013) *Evaluation of Enzyme Inhibitors in Drug Discovery*
Second Edition, J. Wiley, New York, Chapter 9 (sect. 9.1)

Reaction progress at a given inhibitor concentration, $[I]_0$:

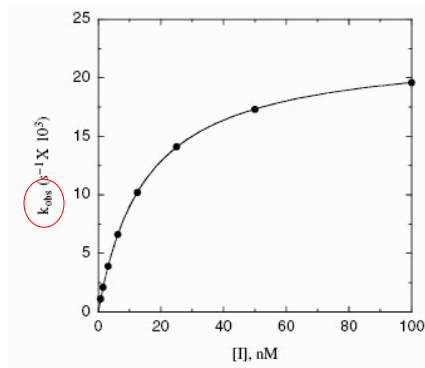


$$[P] = \frac{v_i}{k_{obs}} [1 - \exp(-k_{obs} t)]$$

Determine k_{obs}
as a function of $[I]_0$

“Traditional” method to analyze covalent inhibition data: **Step 2**

Copeland, R. (2013) *Evaluation of Enzyme Inhibitors in Drug Discovery* Second Edition, J. Wiley, New York, Chapter 9 (sect. 9.1)



$$k_{obs} = k_{inact} \frac{[I]_0}{[I]_0 + K_i}$$

Nonlinear fit of k_{obs} values to determine k_{inact} and K_i

“Traditional” method: Underlying theoretical assumptions

1. **Linearity** of control curve

Control progress curve ($[I]_0 = 0$) must be **strictly linear** over time.

2. **No tight binding**

The noncovalent K_i value must be **very much higher than [enzyme]**.

- Both of these assumptions are violated for the inhibitors in our series.
- In fact, assumption #1 above is violated for all assays where $[S]_0 \ll K_M$.

-
- We **cannot use** the “traditional” method of kinetic analysis.

Alternate method: Differential equations (DynaFit software)

Kuzmic, P. (2009) "DynaFit – A software package for enzymology"
Meth. Enzymol. **467**, 247-280

INPUT TEXT:

```
[mechanism]
E + S ----> E + P      :   ksub
E + I <=> E.I          :   kai   kdI
E.I ----> E-I          :   kinact
```

INTERNALLY DERIVED MATHEMATICAL MODEL:

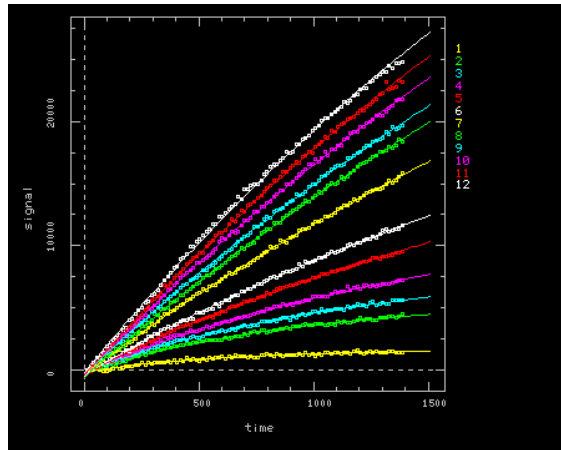
$$\begin{aligned} d[E]/dt &= -k_{\text{sub}}[E][S] + k_{\text{sub}}[E][S] - k_{\text{ai}}[E][I] + k_{\text{di}}[E.I] \\ d[S]/dt &= -k_{\text{sub}}[E][S] \\ d[P]/dt &= +k_{\text{sub}}[E][S] \\ d[I]/dt &= -k_{\text{ai}}[E][I] + k_{\text{di}}[E.I] \\ d[E.I]/dt &= +k_{\text{ai}}[E][I] - k_{\text{di}}[E.I] - k_{\text{inact}}[E.I] \\ d[E-I]/dt &= +k_{\text{inact}}[E.I] \end{aligned}$$

system of
differential equations

solved by using
numerical methods

Differential equation method: Example – Afatinib: Data & model

DYNAFIT-GENERATED OUTPUT



"global fit"

combined
progress
curves
analyzed
together

Beechem, J. M. (1992) "Global analysis of biochemical and biophysical data"
Meth. Enzymol. **210**, 37-54.

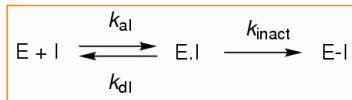
Differential equation method: Example – Afatinib: **Parameters**

DYNAFIT-GENERATED OUTPUT

Optimized Parameters

No.	Par#Set	Initial	Final	Std. Error	CV (%)
#1	k _{sub}	0.02	0.0148823	0.000279397	1.88
#2	k _{dI}	0.06342	0.0314187	0.00188872	6.01
#3	k _{inact}	0.01	0.00204131	0.00016957	8.31
#4	[E]	0.02	0.0192718	0.000358634	1.86

$$K_i = 0.0314 / 10 = \mathbf{0.00314 \mu M}$$



$$K_i = k_{dI} / k_{aI}$$

$$k_{aI} = \mathbf{10 \mu M^{-1} s^{-1}} \dots \text{assumed (fixed constant)}$$

FINAL RESULTS: Afatinib – Replicate 1: $K_i = 3.14 \text{ nM}$
 $k_{inact} = 0.00204 \text{ s}^{-1}$

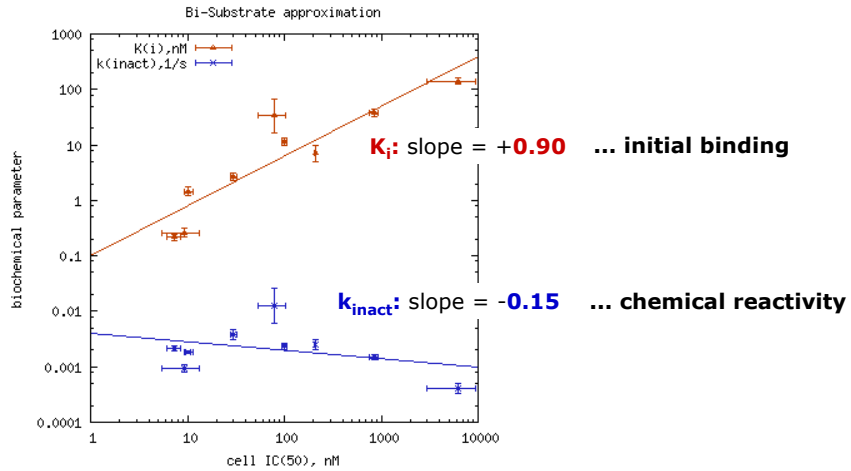
Differential equation method: Example – Afatinib: **Reproducibility**

EACH "REPLICATE" REPRESENT A **SEPARATE PLATE**

	k_{inact} s^{-1}	K_i nM	k_{inact} / K_i $\mu M^{-1} s^{-1}$
Replicate #1	0.0020	3.1	10.4
Replicate #2	0.0021	3.1	10.5
Replicate #3	0.0025	4.0	9.9

Reproducibility ($n=3$) of rate constants **5-15%** for **all compounds**.

Final results: Biochemical activity vs. Cellular potency

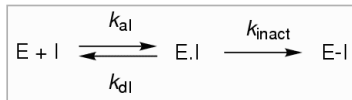


Cellular potency correlates **strongly** with **binding**, but only weakly with reactivity.

**CHECK UNDERLYING ASSUMPTIONS:
BIMOLECULAR ASSOCIATION RATE**

Differential equation method: Example – Afatinib: Parameters

DYNAFIT-GENERATED OUTPUT



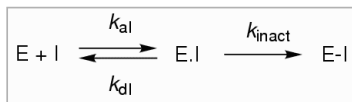
$$K_i = k_{dI} / k_{aI}$$

$$k_{aI} = 10 \mu\text{M}^{-1}\text{s}^{-1} \dots \text{assumed (fixed constant)}$$

recall:
we
assumed
this value

Could the final result be skewed by making an **arbitrary assumption** about the magnitude of the association rate constant?

Varying assumed values of the association rate constant, k_{aI}



EXAMPLE: **Afatinib, Replicate #1/3**

ASSUMED $k_{aI}, \mu\text{M}^{-1}\text{s}^{-1}$	DETERMINED FROM DATA			
	k_{inact}, s^{-1}	k_{dI}, s^{-1}	K_i, nM	$k_{inact}/K_i, \mu\text{M}^{-1}\text{s}^{-1}$
10	0.0016	0.037	3.7	23.1
20	0.0016	0.074	3.7	23.1
40	0.0016	0.148	3.7	23.1

$$K_i = k_{dI} / k_{aI}$$

Effect of **assumed** association rate constant: Conclusions

The assumed value of the "on" rate constant

- **does** effect the best-fit value of the **dissociation** ("off") rate constant, k_{off} .
- The fitted value of k_{off} increases **proportionally** with the assumed value of k_{on} .
- Therefore the best-fit value of the inhibition constant, K_i , **remains invariant**.
- The inactivation rate constant, k_{inact} , remains unaffected.

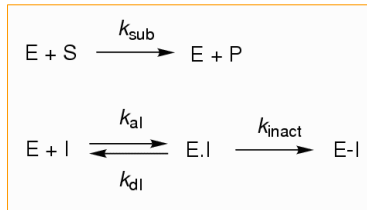
Assumptions about the "on" rate constant have **no effect** on the best-fit values of k_{inact} , K_i , and k_{inact}/K_i .

However, the dissociation ("off") rate constant remains **undefined** by this type of data.

**CHECK UNDERLYING ASSUMPTIONS:
SUBSTRATE MECHANISM**

Substrate mechanism – “Hit and Run”

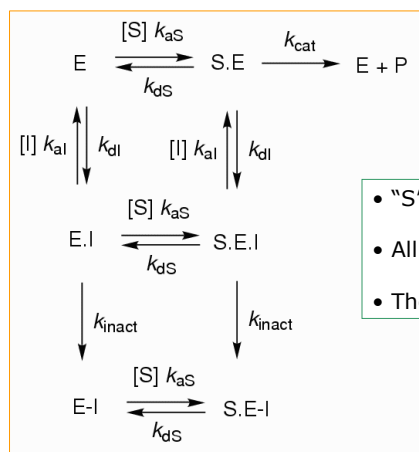
ASSUMING THAT THE MICHAELIS COMPLEX CONCENTRATION IS EFFECTIVELY ZERO



- Justified by assuming that $[S]_0 \ll K_M$
- In our experiments $K_M \geq 220 \mu\text{M}$ and $[S]_0 = 13 \mu\text{M}$
- The model was used in Schwartz *et al.* 2014 (PNAS)

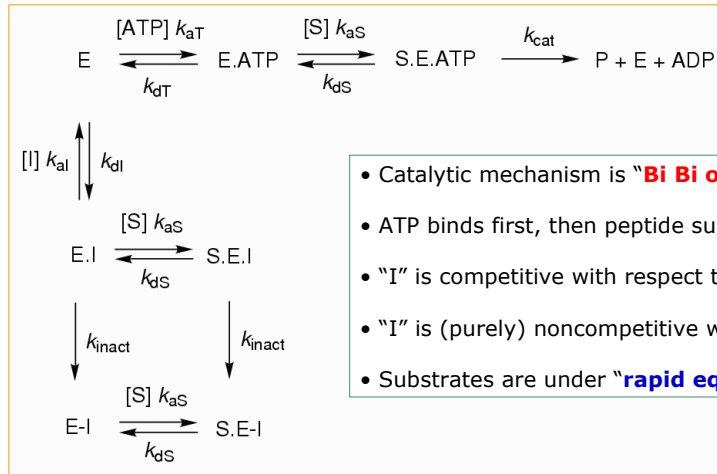
Substrate mechanism – Michaelis-Menten

ASSUMING THAT ATP COMPETITION CAN BE EXPRESSED THROUGH “APPARENT” K_i



- “S” is the **peptide** substrate
- All inhibitors are **ATP-competitive**
- Therefore they are **“S”-noncompetitive**

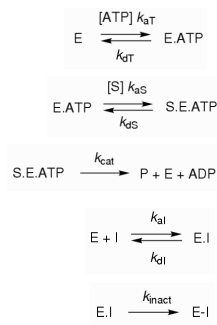
Substrate mechanism – Bi-Substrate



- Catalytic mechanism is "**Bi Bi ordered**"
- ATP binds first, then peptide substrate
- "I" is competitive with respect to ATP
- "I" is (purely) noncompetitive w.r.t. "S"
- Substrates are under "**rapid equilibrium**"

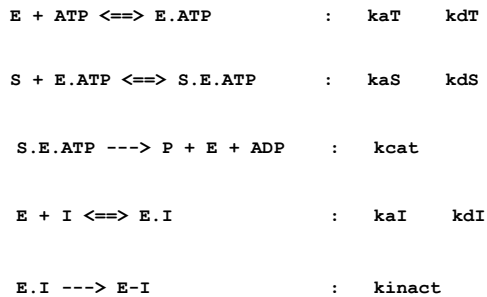
Substrate mechanism – "Bi-Substrate": DynaFit notation

MECHANISM:



DYNAFIT INPUT:

[mechanism]



Similarly for the remaining steps in the mechanism.

Substrate mechanism – “Bi-Substrate”: DynaFit notation

DYNAFIT INPUT WINDOW:

```

DynaFit : fit-progress-global-bs-ci.txt
File Edit View Help
Input Output

[task]
data = progress
task = fit

[mechanism]
E + T <=> E.T      : kaT kdT
S + E.T <=> S.E.T   : kaS kdS
S.E.T ---> P + E + D : keat

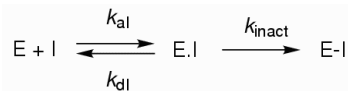
E + I <=> E.I      : kaI kdI
E.I ---> E-I      : kinact

S + E.I <=> S.E.I   : kaS kdS
S.E.I ---> S.E-I   : kinact
S.E-I <=> S + E-I  : kdS kaS

[constants]
bas = 1000
    
```

Presumed substrate mechanisms vs. k_{inact} and K_i

EXAMPLE: AFATINIB, REPLICATE #1/3



	FIXED k_{aI} , $\mu\text{M}^{-1}\text{s}^{-1}$	k_{dI} , s^{-1}	k_{inact} , s^{-1}	k_{dI}/k_{aI} K_i , nM
Hit-and-Run	10	0.031	0.0019	3.1
Michaelis-Menten	10	0.033	0.0019	3.1
Bisubstrate	160	0.032	0.0019	0.19 = 3.1/16

$$[\text{ATP}]/K_{M,\text{ATP}} = 16$$

Substrate mechanism – Summary

1. Basic characteristic of inhibitors (K_i , k_{inact}) are essentially **independent** on the presumed substrate mechanism.
2. The inactivation rate constant (k_{inact}) is **entirely invariant** across all three substrate mechanisms.
3. The initial binding affinity (K_i) needs to be **corrected for ATP** competition in the case of “Hit and Run” and “Michaelis-Menten” mechanisms:
 - **Hit-and-Run** or **Michaelis-Menten**:
Divide the measured K_i^{app} value by $[ATP]/K_{M,ATP}$ to obtain true K_i
 - **Bisubstrate**:
True K_i is obtained directly.

**THE NEXT FRONTIER:
MICROSCOPIC “ON” AND “OFF” RATE CONSTANTS**

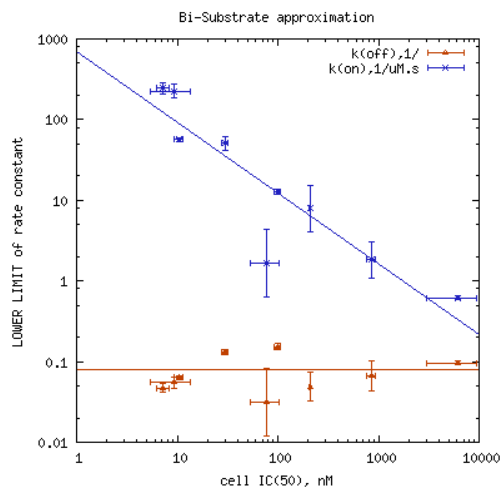
Confidence intervals for “on” / “off” rate constants: Method

- We cannot measure “on” and “off” rate constants *as such*.
- But can estimate at least the **lower limits** of their confidence intervals.

METHOD: **“Likelihood profile”** a.k.a. **“Profile-t”** method

- REFERENCES:
1. Watts, D.G. (1994)
“Parameter estimates from nonlinear models”
Methods in Enzymology, vol. **240**, pp. 23-36
 2. Bates, D. M., and Watts, D. G. (1988)
Nonlinear Regression Analysis and its Applications
John Wiley, New York
sec. 6.1 (pp. 200-216) - two biochemical examples

Confidence intervals for “on” / “off” rate constants: Results



k_{on} : slope = **-0.88**
... **association** rate

k_{off} : slope = **~0.05**
... **dissociation** rate

Cell IC_{50} correlates strongly with **association rates**. Dissociation has no impact.

Cellular potency vs. upper limit of “residence time”

“Drug-receptor residence time”: $\tau = 1 / k_{\text{off}}$

- **Lower** limit for “off” rate constant defines the **upper** limit for residence time.
- Both minimum k_{off} and **maximum τ is invariant** across our compound panel.
- However cellular IC_{50} varies by 3-4 orders of magnitude.

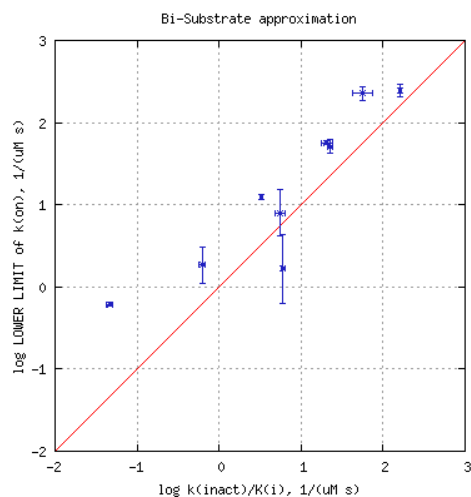
- This is unexpected in light of the “residence time” theory of drug potency:

Copeland, Pompliano & Meek (2006) *Nature Rev. Drug Disc.* **5**, 730

Tummino & Copeland (2008) *Biochemistry* **47**, 5481.

Copeland (2011) *Future Med. Chem.* **3**, 1491

Lower limit for the “on” rate constant vs. k_{inact}/K_i



k_{inact}/K_i from rapid-equilibrium model is a good “proxy” for minimal k_{on} .

Summary and conclusions

1. EQUILIBRIUM BINDING AFFINITY:

Initial (non-covalent) binding seems more important for cell potency than chemical reactivity.

2. BINDING DYNAMICS:

Association rates seem more important for cell potency than dissociation rates (i.e., "residence time").

3. k_{inact} / K_i (rapid-equilibrium) appears to be a good proxy for the lower limit of the "on" rate constant.

This work could **not** have been done using the "usual" data-analysis method:

- substrate depletion ($[S]_0 \ll K_M$)
- inhibitor depletion ($[I]_0 \sim [E]_0$)



use **DynaFit** to analyze covalent inhibition data

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